S to Co coordination in  $\text{Co}_9\text{S}_8$  is that of the Rh(m) with the S(f), S(i) and S(j) atoms. The average distance for these is 2.33 Å (Geller, 1962b) compared with the average tetrahedral Co-S distance, 2.19 Å. Moreover, the relatively longer Rh(m)-Rh(m) than Co(f)-Co(f) distances (Table 4) would imply a relative shortening of Rh(m)-S distances. Thus we are able to conclude that the 4-coordination distances are relatively as one would have predicted.

It is possible that the more complex bonding and packing in the  $Rh_{17}S_{15}$  results in the shortening of the bonds of the single Rh atom in the unit cell having octahedral coordination. By studying the systems in which Co replaces Rh in  $Rh_{17}S_{15}$  and that in which Rh replaces Co in  $Co_9S_8$ , we hope to gain some further insight into the bonding and atom sizes as well as effects on the superconductive properties of  $Rh_{17}S_{15}$ .

### References

- ALSÉN, N. (1925). Geol. Fören. Förhandl. 47, 54.
- BOND, W. L. (1951). Rev. Sci. Instrum. 22, 344.
- BOND, W. L. (1959). Acta Cryst. 12, 375.
- BUSING, W. R. & LEVY, H. (1959). ORNL Central Files Memorandum 59-4-37, April.
- DAUBEN, C. H. & TEMPLETON, D. H. (1955). Acta Cryst. 8, 841.
- DAWSON, B. (1960). Acta Cryst. 13, 403.
- GELLER, S. (1962a). Acta Cryst. 15, 713.
- GELLER, S. (1962b). Acta Cryst. 15, 1198.
- JUZA, R., HÜLSMAN, O., MEISEL, K. & BILTZ, W. (1935). Z. anorg. Chem. 225, 369.
- KERR, P. F. (1945). Amer. Min. 30, 483.
- LINDQVIST, M., LUNDQVIST, D. & WESTGREN, A. (1936). Svensk Kem. Tidsk. 48, 156.
- TAYLOR, A. & FLOYD, R. W. (1950). Acta Cryst. 3, 285.
- THOMAS, L. H. & UMEDA, K. (1957). J. Chem. Phys. 26, 293.
- THOMASSEN, L. (1929). Z. Phys. Chem. (B), 4, 277.

Acta Cryst. (1962). 15, 1198

# The Crystal Structure of the Superconductor Rh<sub>17</sub>S<sub>15</sub>

# BY S. Geller

Bell Telephone Laboratories, Incorporated, Murray Hill, New Jersey, U.S.A.

## (Received 1 March 1962)

Crystals of  $\operatorname{Rh}_{17}\operatorname{S}_{15}$ , isostructural with those of  $\operatorname{Pd}_{17}\operatorname{Se}_{15}$ , belong to one of three space groups  $O_b^1 - Pm3m$ ,  $T_d^1 - P\overline{4}3m$  or  $O^1 - P432$ , have a lattice constant of  $9\cdot911 \pm 0\cdot001$  Å, and two formula units per unit cell. The structure of  $\operatorname{Rh}_{17}\operatorname{S}_{15}$  has been refined in Pm3m from selected single-crystal X-ray data. It is shown that there are relatively short Rh-Rh contacts in  $\operatorname{Rh}_{17}\operatorname{S}_{15}$ .

#### Introduction

To date, only  $Rh_{17}S_{15}$  and  $Pd_{17}Se_{15}$  are known to crystallize with the structure to be described in this paper. A detailed account of the structural study of  $Pd_{17}Se_{15}$  has already been given (Geller, 1962); it was mentioned that X-ray data from both  $Rh_{17}S_{15}$  and  $Pd_{17}Se_{15}$  were useful in the solution of the structural problem. The main purpose of the present paper is to report on the structural details of  $Rh_{17}S_{15}$  and to point out how they differ from those of  $Pd_{17}Se_{15}$ .

The rhodium-sulfur system was first investigated by Juza, Hulsmann, Meisel & Biltz (1935). They found a compound that they designated  $Rh_9S_8$ , which appeared from X-ray powder diffraction data to have primitive cubic symmetry. The compound was found to be superconducting by Matthias, Corenzwit & Miller (1954). Recently, Kjekshus (1960) carried out X-ray studies over a temperature range on compounds alleged to be  $Rh_9S_8$  and  $Pd_9Se_8$ . The structural study has conclusively shown, however, that the correct formulae of the compounds are  $Rh_17S_{15}$  and  $Pd_17Se_{15}$ , as shown in the paper on the latter compound.

#### Experimental

The lattice constant obtained from a powder photograph (taken with a 114.6 mm. diameter Norelco Straumanis camera and using Cu K radiation) of a specimen with an originally intended composition  $Rh_9S_8$  is  $9.911 \pm 0.001$  Å. This value probably represents the lattice constant of Rh<sub>17</sub>S<sub>15</sub> well within experimental error. A compound Rh<sub>9</sub>S<sub>8</sub> would contain 78.31% Rh by weight while Rh<sub>17</sub>S<sub>15</sub> contains 78.44%Rh by weight; the difference is small. Furthermore a specimen made up with intended composition  $Rh_8S_7$ (78.58% Rh) contained elementary rhodium as shown by an X-ray photograph. Excess sulfur would be difficult to see in the 'Rh<sub>9</sub>S<sub>8</sub>.' The phase appears to be fairly sharply defined in the Rh-S system, but even if there were some solution of sulfur in the Rh<sub>17</sub>S<sub>15</sub>, there would probably not be a significant difference in lattice constant between 'Rh<sub>9</sub>S<sub>8</sub>' and Rh<sub>17</sub>S<sub>15</sub>.

With two  $Rh_{17}S_{15}$  in the unit cell, the X-ray density 7.60 g.cm.<sup>-3</sup> is in good agreement with the value 7.68 g.cm.<sup>-3</sup> obtained pycnometrically on an 'Rh<sub>9</sub>S<sub>8</sub>' specimen.

1198

An essentially\* single crystal of irregular shape and less than 0.2 mm. each dimension, was photographed with a Buerger precession camera with the [100] direction as precession axis. Weissenberg photographs were also taken about both the [100] and [110] directions as rotation axes. Mo Kx radiation was used throughout.

The diffraction symmetry was m3m. There were no systematic absences; thus the probable space groups are  $O_h^1 - Pm3m$ ,  $T_d^1 - P\overline{4}3m$  and  $O_1 - P432$ .

The hk0 and hk1 intensity data used in the structure refinement were obtained from the procession photographs; the hkk data used in the refinement were obtained from the Weissenberg photographs, only those reflections for which  $\sin \theta_{hkk} < 0.790$  being included. The intensity estimates were made visually by comparison with a calibrated intensity strip. From the precession-camera data, relative  $|F_{hkl}|^2$ were obtained by applying the Lorentz-polarization corrections as obtained from Waser (1951, 1952) and Grenville-Wells & Abrahams (1952) charts supplied by Nies.<sup>†</sup> Lorentz-polarization corrections were also applied to the Weissenberg data in the usual way. No corrections were made for absorption or extinction.

### **Refinement of the structure**

It has been shown in the paper on Pd<sub>17</sub>Se<sub>15</sub>, that it is not possible to make a choice of the most probable of the three space groups to which the crystal might belong. The lowest standard errors were obtained in the centrosymmetric space group, but this in itself does not necessarily mean that it is the most probable one. In fact, as a result of the work on the  $Pd_{17}Se_{15}$ , the author is led to the speculation that if a structure truly belongs to a non-centrosymmetric space group but is only a very small perturbation on a centrosymmetric one, it is highly probable that it will converge more rapidly in the latter and have lower standard errors on the average. That is, the standard errors for like parameters will be about the same in the two groups, but those which arise from the additional degrees of freedom in the non-centrosymmetric group will have large standard errors associated with them (Geller, 1962). For Rh<sub>17</sub>S<sub>15</sub>, refinement was based only on the centrosymmetric space group Pm3m.

The total number of independent reflections within the precession camera range on the zeroth and first layer photographs about [100] and on the zeroth level Weissenberg photograph about [110] with  $\sin \theta_{hkk} < 0.790$  was 402. Of these, 128 were too weak to be observed.

Refinement was carried out using the IBM 704 Busing-Levy (1959) least-squares program adapted to the IBM 7090 with a compatibility program. At first all reflection amplitudes of observed reflections were given unit weight while those of reflections too weak to be observed were weighted zero. The starting positional parameters were the analogous final parameters of  $Pd_{17}Se_{15}$  except for the Rh atoms in 24m. These were taken as x = 0.360 and z = 0.140 as against 0.352 and 0.150 respectively for Pd<sub>17</sub>Se<sub>15</sub>. The change was based on examination of a number of the amplitudes. Starting values of isotropic temperature factors were 0.10 Å<sup>2</sup> for all Rh atoms and 0.25 Å<sup>2</sup> for all S atoms. In the calculation of structure amplitudes, the atomic scattering factors used for Rh were those of Thomas & Umeda (1957) and for sulfur, those of Dawson (1960). The real part of the dispersion correction (Dauben & Templeton, 1955) was applied to the Rh scattering factors.

Although after the first least-squares cycle there was little change in positional parameters, there was some difficulty with the temperature factors as was also found for Pd<sub>17</sub>Se<sub>15</sub>. In early iterations several of the amplitudes from reflections which suffered heavily from extinction were given zero weight and in subsequent iterations those for which  $|AF| \ge 30$  were given zero weight; the changes in positional parameters were not significant. The temperature factors were more reasonable but several were still negative\* in the last cycle. Examination of the correlation matrix (Geller, 1961) indicates that interactions between the temperature factors and positional parameters are all small and therefore that we may have some confidence in the interatomic distances ealculated from the latter. The final parameters and standard deviations based on the use of 219 amplitudes with unit weight are given in Table 1. Calculated and observed amplitudes with the positional parameters given in Table 1 but with values of B, 0.05 Å<sup>2</sup> for all Rh and 0.10 Å<sup>2</sup> for all S atoms are listed in Table 2. The discrepancy factor including considera-

\* In some of the photographs, some extra spots appeared which were obviously from an occluded crystallite.

† N. P. Nies, 969 Skyline Drive, Laguna Beach, California.

\* However, the standard errors (Table 1) indicate that none of these are significantly different from zero.

Atom	Position	x	y	z	В	$\sigma(x)$	$\sigma(z)$	$\sigma(B)$
$\mathbf{R}\mathbf{h}$	24m	0.3564	0.3564	0.1435	0.01	0.0001	0.0002	0.02
s	12j	0.1696	0.1696	ł	-0.01	0.0006		0.09
S	12i	0.2310	0.2310	õ	0.12	0.0008		0.11
S	6f	$\frac{1}{2}$	1	0.2643	0.14		0.0016	0.12
$\mathbf{R}\mathbf{h}$	6e	Ō	õ	0.2388	-0.05		0.0005	0.07
$\mathbf{R}\mathbf{h}$	3d	0	0	1/2	0.00			0.02
$\mathbf{R}\mathbf{h}$	16	12	12	1	-0.24			0.12

 Table 1. Final parameters and standard errors

### Table 2. Observed and calculated amplitudes

	hkO			hk 1			hkk			hkk			hkk				hkk	
h k	۴。	F c	h k	Fo	Fc	hk	Fo	Fc	h k	۴.	Fc	h k	F <sub>o</sub>	Fc	h	k	۴	F <sub>c</sub>
1234567891011234234567891011233456789101123456789101123567891011267891011267891011278910112892222222222	339 2208 1130228 1130228 11418 53654 10515 58654 10515 587 58654 10515 587 587 58654 10515 587 587 587 587 587 587 587 587 587 58	$\begin{array}{c} - 27\\ 239\\ 237\\ 239\\ 149\\ - 172\\ 115\\ - 174\\ 166\\ 116\\ - 52\\ 9\\ - 111\\ - 915\\ 100\\ 100\\ - 915\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 100\\ 1$	2 3 4 5 6 7 8 9 10 11 21 3 4 5 6 7 8 9 10 11 21 3 4 5 6 7 8 9 10 11 21 3 5 6 7 8 9 10 11 21 7 8 9 10 11 21 3 4 5 6 7 8 9 10 11 21 3 4 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5 5	173334067757781990919040344687810月8960912720265514214892773934870919193258929391985577697731932572 くくく くくくくくくくく くくろいのよう 1000000000000000000000000000000000000	$\begin{array}{c} -1100\\ -92\\ -300\\ -3716\\ -866\\ -166$	00000000000000000000000000000000000000	36495554447221646632745370487716980835075718532049034149668667775560177 212418477216563632745370487716980835075718532049034149668677777777755601773 2 < < < < < < < < < < < < < < < < < < <	- 92 - 2234 - 74181977 - 21234 - 7122 - 21234 - 7122 - 21234 - 7122 - 21235 - 21235 - 21235 - 21245 - 21245 - 21255 -	89101121741516789232344444444444444444444444555555555555	042984440128059227115228480447415208962477905699380446899755211140805922878445228483248617782774947799752152011266104661110 1287844401280937522711522848044741520896247779056993867468997777562115092897678681110 128711280059595227112800497678681110	- 822 - 829 - 964 - 964 - 1537 - 1964 - 1537 - 284 - 1052 - 1052	167666667777777777777777777777778910112141516718234567891011214451617012345678910110101010101010101010101010101010101	くくくくく 77 797876524878888 12217315705248070711892783597752733897152733897152751497878785211577778787878753148544567717 くく、「くく」、「これでは、」」、「これでは、「これでは、「これでは、「これでは、」、「これでは、「これでは、「これでは、「これでは、「これでは、「これでは、「これでは、「これでは、「これでは、「これでは、」」、「これでは、「これでは、「これでは、」、これでは、これでは、これでは、これでは、」、これでは、これでは、これでは、これでは、これでは、これでは、これでは、これでは	- 10 17 - 83 - 5169 - 17 - 83 - 5169 - 17 - 17	11 21314 1516 0 1 23 4 5 6 7 8 9 10 11 23 4 15 16 0 1 2 3 4 5 6 7 8 9 10 11 23 4 0 1 2 3 4 5 6 7 8 9 10 11 2 3 4 5 6 7 8 9 0 1 2 3 4 5 6 7 8 9 10 1 2 3 10 1 2 3 10 1 2 3 10 10 1 2 3 10 10 10 10 10 10 10 10 10 10 10 10 10	000000111111111111111111111111112121212	< 2 1 1 2 1 2 1 2 2 2 2 2 2 2 2 2 2 2 2 2	$\begin{array}{c} 39\\ -286\\ -856\\ -6438\\ -6438\\ -188\\ -287\\ -188\\ -287\\ -193\\ -193\\ -193\\ -129\\ -193\\ -129\\ -193\\ -129\\ -193\\ -129\\ -193\\ -129\\ -193\\ -129\\ -193\\ -129\\ -193\\ -129\\ -193\\ -129\\ -193\\ -129\\ -193\\ -129\\ -193\\ -129\\ -193\\ -129\\ -193\\ -112\\ -288\\ -133\\ -365\\ -183\\ -112\\ -298\\ -132\\ -168\\ -132\\ -298\\ -132\\ -168\\ -132\\ -298\\ -132\\ -288\\ -288\\$

tion of multiplicity but excluding the 600, 800 and 440 amplitudes is 0.12. When the three amplitudes are included, the discrepancy factor is 0.13.

# Description of the structure

The interatomic distances in  $Rh_{17}S_{15}$  are listed in Table 3. For ease of comparison the analogous  $Pd_{17}Se_{15}$  distances are also listed. The general features of the  $Rh_{17}S_{15}$  structure are shown in Fig. 2 of the paper on  $Pd_{17}Se_{15}$  (Geller, 1962). However, in detail, there are important differences in the  $Rh_{17}S_{15}$  and  $Pd_{17}Se_{15}$  structures.

The  $\operatorname{Rh}(b)$ -S(f) are shorter than the  $\operatorname{Rh}(d)$ -S(j)distances (Table 3), even though the former are octahedral whereas the latter *appear* to be squarecoordination distances. This is reverse of the situation in Pd<sub>17</sub>Se<sub>15</sub>. On the other hand, Rh(d) also has two Rh(e) neighbors at 2.59 Å which together with the 4 S(j) atoms completes an octahedron about Rh(d). In Pd<sub>17</sub>Se<sub>15</sub>, the analogous Pd(d)-Pd(e) distance is 2.78 Å, which is 0.03 Å longer than the elementary Pd-Pd distance, 2.75 Å. In elementary Rh which has the same cubic close-packed structure as elementary Pd, the nearest neighbor Rh-Rh distance is 2.69 Å. Thus the Rh(d)-Rh(e) distance in Rh<sub>17</sub>S<sub>15</sub> is 0.10 Å shorter than the elementary Rh-Rh distance, indicating considerably stronger bonding than between the analogous Pd(d)-Pd(e) neighbors. This would account for the longer Rh(d)-S(j) distances.

Further corroboration of the preceding argument is obtained from examination of the Rh-S distances involving Rh(e), which is surrounded by a square of S(i) atoms (though Rh(e) is 0.08 Å out of the plane of the S(i) atoms) and one Rh(d) atom. The Rh(e)-S(i) distance, 2.29 Å, is shorter than that of Rh(b)-S(f), but not in the same proportion as the analogous distances in Pd<sub>17</sub>Se<sub>15</sub>. Again this is justified by the shorter Rh(e)-Rh(d) distance.

The average Rh(m)-S distance is 2.33 Å, not significantly different from the Rh(b)-S(f) distance. This appears to be somewhat anomalous, but again

Atom	Neighbors	Distance	σ	Analogous Pd <sub>17</sub> Se <sub>15</sub> distance
$\mathbf{Rh}(b)$	$6 \operatorname{S}(f)$	2·336 Å	0·016 Å	2·576 Å
$\operatorname{Rh}(d)$	4 S(j) 2 Rh(e)	$2.378 \\ 2.588$	0·009 0·007	$2.527 \\ 2.781$
$\mathrm{Rh}(e)$	4 S(i) 1 Rh(d) 4 Rh(e)	2·291 2·588 3·348	0·008 0·007 0·007	2·438 2·781 3·566
$\operatorname{Rh}(m)$	1 S(i)  1 S(f)  2 S(j)  1 Rh(m)  2 Rh(m)  2 Rh(m)  2 Rh(m)	$2 \cdot 261$ $2 \cdot 342$ $2 \cdot 349$ $2 \cdot 844$ $2 \cdot 846$ $2 \cdot 984$	0.010 0.010 0.006 0.004 0.003 0.003	$2 \cdot 430$ $2 \cdot 492$ $2 \cdot 509$ $3 \cdot 184$ $3 \cdot 137$ $3 \cdot 029$
S(f)	$\begin{array}{c} 4 \; { m S}(f) \ 4 \; { m S}(j) \ 4 \; { m Rh}(m) \ 1 \; { m Rh}(b) \end{array}$	$3.304 \\ 3.406 \\ 2.342 \\ 2.336$	$0.022 \\ 0.012 \\ 0.010 \\ 0.016$	$3.643 \\ 3.641 \\ 2.492 \\ 2.576$
S(i)	$\begin{array}{c} 4 \; { m S}(i) \ 4 \; { m S}(j) \ 2 \; { m Rh}(e) \ 2 \; { m Rh}(m) \end{array}$	3·238 3·210 2·291 2·261	0-009 0-007 0-008 0-010	3·445 3·440 2·438 2·430
$\mathbf{S}(j)$	2 S(f) 4 S(i) 2 S(j) 1 Rh(d) 4 Rh(m)	3·406 3·210 3·362 2·378 2·349	0.012 0.007 0.013 0.009 0.006	3.641 3.440 3.572 2.527 2.509

Table 3. Interatomic distances and standard error in Rh17S15

examination of the metal-metal distances indicates a possible reason. The three nearest Rh(m)-Rh(m)distances, although 0.16 Å longer than the elementary distances, are relatively considerably shorter than the analogous Pd-Pd distances; the nearest neighbor Pd(m)-Pd(m) distances average 3.15 Å which is 0.40 Å longer than the elementary distance. Thus it appears that in Rh<sub>17</sub>S<sub>15</sub> the Rh-Rh bonds are in general stronger than the Pd-Pd bonds in Pd<sub>17</sub>Se<sub>15</sub>.

#### References

- BUSING, W. R. & LEVY, H. (1959). ORNL Central Files Memorandum 59-4-37, April.
- DAUBEN, C. H. & TEMPLETON, D. H. (1955). Acta Cryst. 8, 841.
- DAWSON, B. (1960). Acta Cryst. 13, 403.
- GELLER, S. (1954). J. Amer. Chem. Soc. 77, 2641.
- GELLER, S. (1961). Acta Cryst. 14, 1026.
- Geller, S. (1962). Acta Cryst. 15, 713.
- GRENVILLE-WELLS, H. J. & ABRAHAMS, S. C. (1952). Rev. Sci. Instrum. 23, 328.
- JUZA, R., HÜLSMAN, O., MEISEL, K. & BILTZ, W. (1935). Z. anorg. Chem. 225, 369.
- KJEKSHUS, A. (1960). Acta Chem. Scand. 14, 1623.
- THOMAS, L. H. & UMEDA, K. (1957). J. Chem. Phys. 26, 293.
- WASER, J. (1951). Rev. Sci. Instrum. 22, 567.
- WASER, J. (1952). Rev. Sci. Instrum. 23, 430.

### Acta Cryst. (1962). 15, 1201

# Neutron Diffraction Study of Ammonium Perchlorate

# BY H. G. SMITH AND H. A. LEVY

Chemistry Division, Oak Ridge National Laboratory,\* Oak Ridge, Tennessee, U.S.A.

### (Received 30 October 1961)

A neutron diffraction study of single crystals of NH<sub>4</sub>ClO<sub>4</sub> at room temperature has indicated that the orientation of the ammonium ion in the crystal is random, and suggests that it is undergoing free or nearly free rotation.

### Introduction

A room temperature single crystal study of ammonium perchlorate was undertaken in order to compare the structure of this compound with the 'isomorphous' compound hydronium perchlorate (also under investigation by the authors). A structure comprising an ordered, hydrogen-bonded arrangement of the ammonium ions had been suggested from X-ray

difference Fourier projections by Venkatesan (1957). This arrangement, however, is not consistent with the present neutron data which suggests that the ammonium ion is undergoing essentially free rotation. The recent infra-red (Waddington, 1958), nuclear magnetic resonance (NMR) (Ibers, 1960, and Richards & Schaefer, 1961), heat capacity (Justice & Westrum, 1961) and cold neutron (Rush, Taylor & Havens, 1961) studies strongly support these results. The OH<sub>3</sub>ClO<sub>4</sub> neutron diffraction study in which the  $OH_3^+$  ion is disordered, but not rotating, will be reported at a later date.

<sup>\*</sup> Operated for the U.S. Atomic Energy Commission by Union Carbide Corporation.